Computer Simulations and Nanotechnology

Intro:

- Making use of high speed modern computers, and therefore nanotechnology
- Contributing to the development of nanotechnology

Tools:

- A. Starting from basic equations of physics, predict the properties of chemicals such as structure, stability and transitions
- B. Gain intuition and insight, useful when designing experiments

Applications:

- 1. Metal overlayer growth, formation of nanostructures
- 2. Clustering of boron dopant atoms in semiconductors
- 3. New methods for ammonia synthesis, nanopatterned catalysts

# **Computer Simulations**

A new approach to scientific research



Simulations based on basic equations of phyiscs are capable of predicting the properties of new materials

Necessarily approximate and needs to be tested against experiments on similar systems

Can be used to screen ideas, prioritize more expensive experimental research

in vitro ---- in vivo ----- in silico

#### First principles (ab initio) calculations

Paul Dirac, 1929:

The fundamental laws necessary for the mathematical treatment of large parts of physics and the whole of chemistry are thus fully known, and the difficulty lies only in the fact that application of these laws leads to equations that are too complex to be solved'.

Nobel price in Chemistry in 1998 went to Kohn and Pople for the development of methods to solve these equations in an approximate way. Can use to find energy and atomic forces  $E(R_1, R_2, ..., R_N)$  and  $F_i = -\partial E/\partial x_i$ 

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#### **Time scale problem:**

- Most interesting transitions are rare events (ie, much slower than vibrations).
- A transition with an energy barrier of 0.5 eV and a typical prefactor occurs 1000 times per second at room temperature. A direct classical dynamics simulation would require 10<sup>12</sup> force evaluations and thousands of years of CPU time to cover the average time period between such events.



### Cannot simply heat the system, the mechanism can change!

# A walk on the potential energy surface $E(R1,R_2,...,R_N)$ Use Transition State Theory wich assumes

- 1. Born-Oppenheimer
- 2. Classical dynamics for nuclei
- 3. Boltzmann distribution in R
- 4. No recrossings of TS

#### Result:

$$k^{TST} = \frac{\langle v_{\perp} \rangle}{2} \frac{Q^{TS}}{Q^{Initial}}$$

- TST gives the lifetime, τ=1/k, of a given initial state, no knowledge of final state(s)
  Need to run (short time) dynamics starting from TS to find the final state(s)
- Such trajectories can be used to take recrossings into account dynamical corrections

$$k = \kappa k^{TST}$$



An example of unexpected mechanism (P. Feibelman 1990) diffusion of an Al adatom on an Al(100) surface



Note: The final state is different in the two cases!

#### Instead of guessing, FIND relevant processes from atomic forces:

Within HTST, need to find all the relevant saddle points



Min mode method searches for saddle points



#### **Distributed long time scale simulations of solids**



#### **Adatom diffusion on Al(100)**

**Compare EAM with DFT** 



#### **Statistics**

temperature: 300 K total transitions: 1000 distinct transitions: 112 total time: 55 ns dimer searches per step: 50 distinct processes per step: 15



$$\Delta E = 0.23 \text{ eV} (0.24 \text{ eV})$$
$$\nu = 7 \cdot 10^{13} \text{ s}^{-1} (1 \cdot 10^{14} \text{ s}^{-1})$$



 $\Delta E = 0.37 \text{ eV} (0.52 \text{ eV})$  $\nu = 5 \cdot 10^{13} \text{ s}^{-1} (7 \cdot 10^{13} \text{ s}^{-1})$ 



 $\Delta E = 0.41 \text{ eV} (0.50 \text{ eV})$  $v = 2 \cdot 10^{15} \text{ s}^{-1} (8 \cdot 10^{14} \text{ s}^{-1})$ 



 $\Delta E = 0.44 \text{ eV}$  $v = 3 \cdot 10^{14} \text{ s}^{-1}$ 

#### Long time dynamics: Ripening on Al(100)







n = 1 t = 0 ns

n = 10 t = 6 ns





#### **Statistics**

temperature: 300K total transitions: 129,000 distinct transitions: 341 total time: 1 ms dimer searches per step: 50 distinct processes per step: 26 n = 344 t = 70 ns

n = 1000 t = 8 µs





n = 7902 t = 10 μs

n = 65720 t = 1 ms

#### Simulate deposition of atoms on a surface

Deposition event creates a local hot spot that cools down in ca. 1 ps

#### 'Landslide'occurs in this case







## **Compare Al(100) and Cu(100) crystal growth**

Aluminum grows much smoother than copper at 80K, largely because of multi-atom smoothening events









#### **Pyramids on Al(110)**

#### Simulations: EON screen saver

10 layers of atoms have been deposited in ten milliseconds at a temperature of 80K



Experiments: Valbusa et. al. (Genoa)



## Growth of metal islands on MgO (model catalyst) **Catlytic properties depend strongly on size and shape of islands**



Side View





2D Island



**3D** Island







**0.7 ps** 



**2 ps** 

**0 ps** 

#### **Another application of AKMC: Boron clustering in silicon**

As semiconductor devices become smaller, dopant concentration needs to be increased to give the same electric current throughput

Boron concentration has become high enough that clusters form after implantation and low T annealing. The boron clusters are not active

High temperature, short time annealing is used to dissociate boron clusters and re-activate the dopant

It is important to understand how dopant clusters form and dissociate, and what their properties are

Rates of dopant clustering/dissolution are needed as input parameters for modeling device manufacturing.



#### **Calculations:** Possible B<sub>3</sub>I<sup>-</sup> cluster breakup processes, Step 1

1. 
$$U_{SP} = 1.5 \text{ eV}$$
  
 $U_{MIN} = 1.5 \text{ eV}$   
2.  $U_{SP} = 1.5 \text{ eV}$   
 $U_{MIN} = 2.6 \text{ eV}$   
 $U_{MIN} = 2.1 \text{ eV}$   
3.  $U_{SP} = 1.9 \text{ eV}$   
 $U_{MIN} = 1.7 \text{ eV}$ 

Direct breakup of the highly stable B<sub>3</sub>I<sup>-</sup> cluster: High activation barrier







Further breakup of  $B_2I$ : Overall activation energy 3.0 eV



# New catalyst for ammonia synthesis

The essential step of fertilizer production

Industrial plants today use a method that is more than 100 years old



The N-N triple bond is broken in the beginning, a rate limiting step

Nitrogen fixing bacteria (on the roots of lupine, for example) Enzyme nitrogenase



The N-N bond is the last to be broken, addition of first proton is the rate limiting step Can nanotechnology be used to pattern a Fe surface to catalyze ammonia production along the same route as nitrogenase? Use applied voltage to pump electrons onto  $N_2$  molecule



Future vision: Create small rods that can produce fertilizer using sunlight, water and air. Stick one down with each plant! EU funded collaboration with Jens Norskov at DTU, Denmark

#### Summary

- The Adaptive KMC method can be used to simulate long time scale dynamics. Within harmonic transition state theory, saddle point searches using Min Mode method typically require 400 force evaluations and a few tens to hundreds of saddle point searches started in random directions can suffice to simulate long time scale dynamics with reasonable accuracy.
- When full TST is needed, an optimal TS dividing surface can be found by using the variational principle. This can reveal the mechanism of transitions as well as giving an estimate of the rate. OH-TST is a step in that direction, limited to hyperplane representation of TS. In the case of Al adatom diffusion, the optimization of the orientation of the hyperplane converged to the lower energy exchange mechanism, while initially the hyperplane was set up for the hop mechanism.

# Acknowledgements

VASP code

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# Available software

• Screensaver for long time dynamics:

http://eon.chem.washington.edu

- Template for distributed computing: <u>http://fida.chem.washington.edu</u>
- The software (code plug-ins and additions) for doing dimer, CI-NEB and prefactor calculations with VASP is available from: <u>http://ikazki01.chem.washington.edu/vasp/</u>

## **DFT Calculations of B cluster breakup**

- PW91 GGA functional
- Ultrasoft Pseudo-potentials, 64+ atoms
- Plane waves basis, 2x2x2 k-points





# Search for saddle points of boron cluster breakup processes using the dimer method

- 350 force evaluations per image to find a saddle
- 10 min per force evaluation (IBM Power 2 workst.)
- Of 20 saddle point searches, typically 18 converge to good saddle points
  - 11 yield distinct processes of which 5 might be low in energy

